

# Package ‘FDX’

January 19, 2022

**Type** Package

**Title** False Discovery Exceedance Controlling Multiple Testing Procedures

**Version** 1.0.4

**Date** 2022-01-19

**Maintainer** Florian Junge <florian.junge@h-da.de>

**Language** en-US

**Description** Multiple testing procedures for heterogeneous and discrete tests as described in Döhler and Roquain (2019) <[arXiv:1912.04607v1](https://arxiv.org/abs/1912.04607v1)>. The main algorithms of the paper are available as continuous, discrete and weighted versions.

**License** GPL-3

**Encoding** UTF-8

**Depends** R (>= 3.00), DiscreteFDR

**Imports** Rcpp (>= 1.0.3), methods, PoissonBinomial (>= 1.2.0), pracma

**LinkingTo** Rcpp, PoissonBinomial

**RoxygenNote** 7.1.2

**URL** <https://github.com/DISOhda/FDX>

**BugReports** <https://github.com/DISOhda/FDX/issues>

**NeedsCompilation** yes

**Author** Sebastian Döhler [aut],  
Florian Junge [aut, cre],  
Etienne Roquain [ctb]

**Repository** CRAN

**Date/Publication** 2022-01-19 16:22:53 UTC

## R topics documented:

|                       |   |
|-----------------------|---|
| FDX-package . . . . . | 2 |
| amnesia . . . . .     | 3 |

|                          |    |
|--------------------------|----|
| continuous.GR . . . . .  | 4  |
| continuous.LR . . . . .  | 6  |
| discrete.GR . . . . .    | 8  |
| discrete.LR . . . . .    | 10 |
| discrete.PB . . . . .    | 13 |
| fast.Discrete . . . . .  | 15 |
| hist.FDX . . . . .       | 18 |
| kernel . . . . .         | 19 |
| plot.FDX . . . . .       | 22 |
| print.FDX . . . . .      | 23 |
| rejection.path . . . . . | 24 |
| summary.FDX . . . . .    | 26 |
| weighted.GR . . . . .    | 27 |
| weighted.LR . . . . .    | 29 |
| weighted.PB . . . . .    | 31 |

|              |           |
|--------------|-----------|
| <b>Index</b> | <b>34</b> |
|--------------|-----------|

---

|             |  |
|-------------|--|
| FDX-package | <i>False Discovery Exceedance (FDX) Control for Heterogeneous and Discrete Tests</i> |
|-------------|--|

---

## Description

This package implements the [HLR], [HGR] and [HPB] procedures for both heterogeneous and discrete tests (see Reference).

## Details

The functions are reorganized from the reference paper in the following way. `discrete.LR` (for Discrete Lehmann-Romano) implements [DLR], `discrete.GR` (for Discrete Guo-Romano) implements [DGR] and `discrete.PB` (for Discrete Poisson-Binomial) implements [DPB]. DLR and NDLR are wrappers for `discrete.LR` to access [DLR] and its non-adaptive version directly. Likewise, DGR, NDGR, DPB and NDPB are wrappers for `discrete.GR` and `discrete.PB`, respectively. Their main parameters are a vector of raw observed p-values and a list of the same length, whose elements are the discrete supports of the CDFs of the p-values.

In the same fashion, `weighted.LR` (for Weighted Lehmann-Romano), `weighted.GR` (for Weighted Guo-Romano) and `weighted.PB` (for Weighted Poisson-Binomial) implement [wLR], [wGR] and [wPB], respectively. They also possess wrapper functions, namely `wLR.AM`, `wGR.AM` and `wPB.AM` for arithmetic weighting, and `wLR.GM`, `wPB.GM` and `wPB.GM` for geometric weighting.

The functions `fast.Discrete.LR`, `fast.Discrete.GR` and `fast.Discrete.PB` are wrappers for [fisher.pvalues.support](#) and `discrete.LR`, `discrete.GR` and `discrete.PB`, respectively, which allow to apply discrete procedures directly to a data set of contingency tables.

## References

S. Döhler and E. Roquain (2019). Controlling False Discovery Exceedance for Heterogeneous Tests. [arXiv:1912.04607v1](#).

---

amnesia

*Amnesia and other drug reactions in the MHRA pharmacovigilance spontaneous reporting system*

---

## Description

For each of 2446 drugs in the MHRA database (column 1), the number of cases with amnesia as an adverse event (column 2), and the number of cases with other adverse event for this drug (column 3). In total, 682648 adverse drug reactions were reported, among them 2044 cases of amnesia.

## Usage

```
data(amnesia)
```

## Format

A data frame with 2446 rows representing drugs with the following 3 columns:

**DrugName** The name of the drug.

**AmnesiaCases** Number of the amnesia cases reported for the drug.

**OtherAdverseCases** Number of other adverse drug reactions reported for the drug.

## Details

The data was collected from the Drug Analysis Prints published by the Medicines and Healthcare products Regulatory Agency (MHRA), by Heller & Gur. See references for more details.

## References

R. Heller and H. Gur (2011). False discovery rate controlling procedures for discrete tests. [arXiv:1112.4627v2](#).

## Source

[Drug Analysis Prints on MHRA site](#)

## Examples

```
data.amnesia <- amnesia[, 2:3]
DGR.amnesia <- fast.Discrete.GR(counts = data.amnesia, input = "HG2011")
summary(DGR.amnesia)
```

---

 continuous.GR

*Continuous Guo-Romano procedure*


---

### Description

Apply the usual continuous [GR] procedure, with or without computing the critical values, to a set of p-values. A non-adaptive version is available as well.

### Usage

```
continuous.GR(
  raw.pvalues,
  alpha = 0.05,
  zeta = 0.5,
  adaptive = TRUE,
  critical.values = FALSE
)
```

```
GR(raw.pvalues, alpha = 0.05, zeta = 0.5, critical.values = FALSE)
```

```
NGR(raw.pvalues, alpha = 0.05, zeta = 0.5, critical.values = FALSE)
```

### Arguments

|                 |   |
|-----------------|---|
| raw.pvalues     | vector of the raw observed p-values, as provided by the end user and before matching with their nearest neighbor in the CDFs supports.                      |
| alpha           | the target FDP, a number strictly between 0 and 1. For *.fast kernels, it is only necessary, if stepUp = TRUE.  |
| zeta            | the target probability of not exceeding the desired FDP, a number strictly between 0 and 1. If zeta=NULL (the default), then zeta is chosen equal to alpha. |
| adaptive        | a boolean specifying whether to conduct an adaptive procedure or not.   |
| critical.values | a boolean. If TRUE, critical constants are computed and returned (this is computationally intensive).   |

### Details

GR and NGR are wrapper functions for continuous.GR. The first one simply passes all its parameters to continuous.GR with adaptive = TRUE and NGR does the same with adaptive = FALSE.

### Value

A FDx S3 class object whose elements are:

|          |                                 |
|----------|---------------------------------|
| Rejected | Rejected raw p-values.          |
| Indices  | Indices of rejected hypotheses. |

|                        |   |
|------------------------|---|
| Num.rejected           | Number of rejections.   |
| Adjusted               | Adjusted p-values (only for step-down direction).   |
| Critical.values        | Critical values (if requested).   |
| Method                 | A character string describing the used algorithm, e.g. 'Discrete Lehmann-Romano procedure (step-up)'.                     |
| FDP.threshold          | FDP threshold alpha.  |
| Exceedance.probability | Probability zeta of FDP exceeding alpha; thus, FDP is being controlled at level alpha with confidence $1 - \text{zeta}$ . |
| Adaptive               | A boolean specifying whether an adaptive procedure was conducted or not.  |
| Data\$raw.pvalues      | The values of raw.pvalues.  |
| Data\$data.name        | The respective variable names of raw.pvalues and pCDFlist.  |

**See Also**

[kernel](#), [FDX-package](#), [continuous.LR](#), [discrete.LR](#), [discrete.GR](#), [discrete.PB](#), [weighted.LR](#), [weighted.GR](#), [weighted.PB](#)

**Examples**

```
X1 <- c(4, 2, 2, 14, 6, 9, 4, 0, 1)
X2 <- c(0, 0, 1, 3, 2, 1, 2, 2, 2)
N1 <- rep(148, 9)
N2 <- rep(132, 9)
Y1 <- N1 - X1
Y2 <- N2 - X2
df <- data.frame(X1, Y1, X2, Y2)
df

# Construction of the p-values and their supports (fisher.pvalues.support
# is from 'DiscreteFDR' package!)
df.formatted <- fisher.pvalues.support(counts = df, input = "noassoc")
raw.pvalues <- df.formatted$raw
pCDFlist <- df.formatted$support

GR.fast <- GR(raw.pvalues)
summary(GR.fast)

GR.crit <- GR(raw.pvalues, critical.values = TRUE)
summary(GR.crit)

NGR.fast <- NGR(raw.pvalues)
summary(NGR.fast)

NGR.crit <- NGR(raw.pvalues, critical.values = TRUE)
summary(NGR.crit)
```

---

 continuous.LR

*Continuous Lehmann-Romano procedure*


---

### Description

Apply the usual (continuous) [LR] procedure, with or without computing the critical values, to a set of p-values. A non-adaptive version is available as well.

### Usage

```
continuous.LR(
  raw.pvalues,
  alpha = 0.05,
  zeta = 0.5,
  adaptive = TRUE,
  critical.values = FALSE
)
```

```
LR(raw.pvalues, alpha = 0.05, zeta = 0.5, critical.values = FALSE)
```

```
NLR(raw.pvalues, alpha = 0.05, zeta = 0.5, critical.values = FALSE)
```

### Arguments

|                 |   |
|-----------------|---|
| raw.pvalues     | vector of the raw observed p-values, as provided by the end user and before matching with their nearest neighbor in the CDFs supports.                      |
| alpha           | the target FDP, a number strictly between 0 and 1. For *.fast kernels, it is only necessary, if stepUp = TRUE.  |
| zeta            | the target probability of not exceeding the desired FDP, a number strictly between 0 and 1. If zeta=NULL (the default), then zeta is chosen equal to alpha. |
| adaptive        | a boolean specifying whether to conduct an adaptive procedure or not.   |
| critical.values | a boolean. If TRUE, critical constants are computed and returned (this is computationally intensive).   |

### Details

LR and NLR are wrapper functions for continuous.LR. The first one simply passes all its parameters to continuous.LR with adaptive = TRUE and NLR does the same with adaptive = FALSE.

### Value

A FDx S3 class object whose elements are:

|          |                                 |
|----------|---------------------------------|
| Rejected | Rejected raw p-values.          |
| Indices  | Indices of rejected hypotheses. |

|                        |   |
|------------------------|---|
| Num.rejected           | Number of rejections.   |
| Adjusted               | Adjusted p-values (only for step-down direction).   |
| Critical.values        | Critical values (if requested).   |
| Method                 | A character string describing the used algorithm, e.g. 'Discrete Lehmann-Romano procedure (step-up)'.                     |
| FDP.threshold          | FDP threshold alpha.  |
| Exceedance.probability | Probability zeta of FDP exceeding alpha; thus, FDP is being controlled at level alpha with confidence $1 - \text{zeta}$ . |
| Adaptive               | A boolean specifying whether an adaptive procedure was conducted or not.  |
| Data\$raw.pvalues      | The values of raw.pvalues.  |
| Data\$data.name        | The respective variable names of raw.pvalues and pCDFlist.  |

**See Also**

[kernel](#), [FDX-package](#), [continuous.GR](#), [discrete.LR](#), [discrete.GR](#), [discrete.PB](#), [weighted.LR](#), [weighted.GR](#), [weighted.PB](#)

**Examples**

```
X1 <- c(4, 2, 2, 14, 6, 9, 4, 0, 1)
X2 <- c(0, 0, 1, 3, 2, 1, 2, 2, 2)
N1 <- rep(148, 9)
N2 <- rep(132, 9)
Y1 <- N1 - X1
Y2 <- N2 - X2
df <- data.frame(X1, Y1, X2, Y2)
df

# Construction of the p-values and their supports (fisher.pvalues.support
# is from 'DiscreteFDR' package!)
df.formatted <- fisher.pvalues.support(counts = df, input = "noassoc")
raw.pvalues <- df.formatted$raw
pCDFlist <- df.formatted$support

LR.fast <- LR(raw.pvalues)
summary(LR.fast)

LR.crit <- LR(raw.pvalues, critical.values = TRUE)
summary(LR.crit)

NLR.fast <- NLR(raw.pvalues)
summary(NLR.fast)

NLR.crit <- NLR(raw.pvalues, critical.values = TRUE)
summary(NLR.crit)
```

---

 discrete.GR

*Discrete Guo-Romano procedure*


---

### Description

Apply the [DGR] procedure, with or without computing the critical values, to a set of p-values and their discrete support. A non-adaptive version is available as well.

### Usage

```
discrete.GR(
  raw.pvalues,
  pCDFlist,
  alpha = 0.05,
  zeta = 0.5,
  adaptive = TRUE,
  critical.values = FALSE
)
```

```
DGR(raw.pvalues, pCDFlist, alpha = 0.05, zeta = 0.5, critical.values = FALSE)
```

```
NDGR(raw.pvalues, pCDFlist, alpha = 0.05, zeta = 0.5, critical.values = FALSE)
```

### Arguments

|                 |   |
|-----------------|---|
| raw.pvalues     | vector of the raw observed p-values, as provided by the end user and before matching with their nearest neighbor in the CDFs supports.  |
| pCDFlist        | a list of the supports of the CDFs of the p-values. Each support is represented by a vector that must be in increasing order.   |
| alpha           | the target FDP, a number strictly between 0 and 1. For <code>*</code> fast kernels, it is only necessary, if <code>stepUp = TRUE</code> .   |
| zeta            | the target probability of not exceeding the desired FDP, a number strictly between 0 and 1. If <code>zeta=NULL</code> (the default), then <code>zeta</code> is chosen equal to <code>alpha</code> . |
| adaptive        | a boolean specifying whether to conduct an adaptive procedure or not.   |
| critical.values | a boolean. If <code>TRUE</code> , critical constants are computed and returned (this is computationally intensive).   |

### Details

DGR and NDGR are wrapper functions for `discrete.GR`. The first one simply passes all its parameters to `discrete.GR` with `adaptive = TRUE` and NDGR does the same with `adaptive = FALSE`.



**Value**

A FDX S3 class object whose elements are:

|                        |   |
|------------------------|---|
| Rejected               | Rejected raw p-values.  |
| Indices                | Indices of rejected hypotheses.   |
| Num.rejected           | Number of rejections.   |
| Adjusted               | Adjusted p-values (only for step-down direction).   |
| Critical.values        | Critical values (if requested).   |
| Method                 | A character string describing the used algorithm, e.g. 'Discrete Lehmann-Romano procedure (step-up)'.                     |
| FDP.threshold          | FDP threshold alpha.  |
| Exceedance.probability | Probability zeta of FDP exceeding alpha; thus, FDP is being controlled at level alpha with confidence $1 - \text{zeta}$ . |
| Adaptive               | A boolean specifying whether an adaptive procedure was conducted or not.  |
| Data\$raw.pvalues      | The values of raw.pvalues.  |
| Data\$pCDFlist         | The values of pCDFlist.   |
| Data\$data.name        | The respective variable names of raw.pvalues and pCDFlist.  |

**References**

S. Döhler and E. Roquain (2019). Controlling False Discovery Exceedance for Heterogeneous Tests. [arXiv:1912.04607v1](https://arxiv.org/abs/1912.04607v1).

**See Also**

[kernel](#), [FDX-package](#), [continuous.LR](#), [continuous.GR](#), [discrete.LR](#), [discrete.PB](#), [weighted.LR](#), [weighted.GR](#), [weighted.PB](#)

**Examples**

```
X1 <- c(4, 2, 2, 14, 6, 9, 4, 0, 1)
X2 <- c(0, 0, 1, 3, 2, 1, 2, 2, 2)
N1 <- rep(148, 9)
N2 <- rep(132, 9)
Y1 <- N1 - X1
Y2 <- N2 - X2
df <- data.frame(X1, Y1, X2, Y2)
df

# Construction of the p-values and their supports (fisher.pvalues.support
# is from 'DiscreteFDR' package!)
df.formatted <- fisher.pvalues.support(counts = df, input = "noassoc")
raw.pvalues <- df.formatted$raw
pCDFlist <- df.formatted$support
```

```
DGR.fast <- DGR(raw.pvalues, pCDFlist)
summary(DGR.fast)

DGR.crit <- DGR(raw.pvalues, pCDFlist, critical.values = TRUE)
summary(DGR.crit)

NDGR.fast <- NDGR(raw.pvalues, pCDFlist)
summary(NDGR.fast)

NDGR.crit <- NDGR(raw.pvalues, pCDFlist, critical.values = TRUE)
summary(NDGR.crit)
```

---

discrete.LR

*Discrete Lehmann-Romano procedure*

---

### Description

Apply the [DLR] procedure, with or without computing the critical values, to a set of p-values and their discrete support. Both step-down and step-up procedures can be computed and non-adaptive versions are available as well.

### Usage

```
discrete.LR(
  raw.pvalues,
  pCDFlist,
  alpha = 0.05,
  zeta = 0.5,
  direction = "sd",
  adaptive = TRUE,
  critical.values = FALSE
)
```

```
DLR(
  raw.pvalues,
  pCDFlist,
  alpha = 0.05,
  zeta = 0.5,
  direction = "sd",
  critical.values = FALSE
)
```

```
NDLR(
  raw.pvalues,
  pCDFlist,
  alpha = 0.05,
```

```

    zeta = 0.5,
    direction = "sd",
    critical.values = FALSE
  )

```

### Arguments

|                              |   |
|------------------------------|---|
| <code>raw.pvalues</code>     | vector of the raw observed p-values, as provided by the end user and before matching with their nearest neighbor in the CDFs supports.  |
| <code>pCDFlist</code>        | a list of the supports of the CDFs of the p-values. Each support is represented by a vector that must be in increasing order.   |
| <code>alpha</code>           | the target FDP, a number strictly between 0 and 1. For <code>*.fast</code> kernels, it is only necessary, if <code>stepUp = TRUE</code> .   |
| <code>zeta</code>            | the target probability of not exceeding the desired FDP, a number strictly between 0 and 1. If <code>zeta=NULL</code> (the default), then <code>zeta</code> is chosen equal to <code>alpha</code> . |
| <code>direction</code>       | a character string specifying whether to conduct a step-up ( <code>direction="su"</code> , the default) or step-down procedure ( <code>direction="sd"</code> ).                                     |
| <code>adaptive</code>        | a boolean specifying whether to conduct an adaptive procedure or not.   |
| <code>critical.values</code> | a boolean. If <code>TRUE</code> , critical constants are computed and returned (this is computationally intensive).   |

### Details

DLR and NDLR are wrapper functions for `discrete.LR`. The first one simply passes all its parameters to `discrete.LR` with `adaptive = TRUE` and NDLR does the same with `adaptive = FALSE`.

### Value

A FDX S3 class object whose elements are:

|                                     |  |
|-------------------------------------|--|
| <code>Rejected</code>               | Rejected raw p-values.   |
| <code>Indices</code>                | Indices of rejected hypotheses.  |
| <code>Num.rejected</code>           | Number of rejections.  |
| <code>Adjusted</code>               | Adjusted p-values (only for step-down direction).  |
| <code>Critical.values</code>        | Critical values (if requested).  |
| <code>Method</code>                 | A character string describing the used algorithm, e.g. 'Discrete Lehmann-Romano procedure (step-up)'   |
| <code>FDP.threshold</code>          | FDP threshold <code>alpha</code> .   |
| <code>Exceedance.probability</code> | Probability <code>zeta</code> of FDP exceeding <code>alpha</code> ; thus, FDP is being controlled at level <code>alpha</code> with confidence $1 - zeta$ . |
| <code>Data\$raw.pvalues</code>      | The values of <code>raw.pvalues</code> .   |
| <code>Data\$pCDFlist</code>         | The values of <code>pCDFlist</code> .  |
| <code>Data\$data.name</code>        | The respective variable names of <code>raw.pvalues</code> and <code>pCDFlist</code> .  |

## References

S. Döhler and E. Roquain (2019). Controlling False Discovery Exceedance for Heterogeneous Tests. [arXiv:1912.04607v1](https://arxiv.org/abs/1912.04607v1).

## See Also

[kernel](#), [FDX-package](#), [continuous.LR](#), [continuous.GR](#), [discrete.GR](#), [discrete.PB](#), [weighted.LR](#), [weighted.GR](#), [weighted.PB](#)

## Examples

```
X1 <- c(4, 2, 2, 14, 6, 9, 4, 0, 1)
X2 <- c(0, 0, 1, 3, 2, 1, 2, 2, 2)
N1 <- rep(148, 9)
N2 <- rep(132, 9)
Y1 <- N1 - X1
Y2 <- N2 - X2
df <- data.frame(X1, Y1, X2, Y2)
df

# Construction of the p-values and their supports (fisher.pvalues.support
# is from 'DiscreteFDR' package!)
df.formatted <- fisher.pvalues.support(counts = df, input = "noassoc")
raw.pvalues <- df.formatted$raw
pCDFlist <- df.formatted$support

DLR.sd.fast <- DLR(raw.pvalues, pCDFlist)
summary(DLR.sd.fast)
DLR.su.fast <- DLR(raw.pvalues, pCDFlist, direction = "su")
summary(DLR.su.fast)

DLR.sd.crit <- DLR(raw.pvalues, pCDFlist, critical.values = TRUE)
summary(DLR.sd.crit)
DLR.su.crit <- DLR(raw.pvalues, pCDFlist, direction = "su", critical.values = TRUE)
summary(DLR.su.crit)

NDLR.sd.fast <- NDLR(raw.pvalues, pCDFlist)
summary(NDLR.sd.fast)
NDLR.su.fast <- NDLR(raw.pvalues, pCDFlist, direction = "su")
summary(NDLR.su.fast)

NDLR.sd.crit <- NDLR(raw.pvalues, pCDFlist, critical.values = TRUE)
summary(NDLR.sd.crit)
NDLR.su.crit <- NDLR(raw.pvalues, pCDFlist, direction = "su", critical.values = TRUE)
summary(NDLR.su.crit)
```

---

discrete.PB

*Discrete Poisson-Binomial procedure*


---

### Description

Apply the [DPB] procedure, with or without computing the critical values, to a set of p-values and their discrete support. A non-adaptive version is available as well. Additionally, the user can choose between exact computation of the Poisson-Binomial distribution or a refined normal approximation.

### Usage

```
discrete.PB(
  raw.pvalues,
  pCDFlist,
  alpha = 0.05,
  zeta = 0.5,
  adaptive = TRUE,
  critical.values = FALSE,
  exact = TRUE
)
```

```
DPB(
  raw.pvalues,
  pCDFlist,
  alpha = 0.05,
  zeta = 0.5,
  critical.values = FALSE,
  exact = TRUE
)
```

```
NDPB(
  raw.pvalues,
  pCDFlist,
  alpha = 0.05,
  zeta = 0.5,
  critical.values = FALSE,
  exact = TRUE
)
```

### Arguments

|             |   |
|-------------|---|
| raw.pvalues | vector of the raw observed p-values, as provided by the end user and before matching with their nearest neighbor in the CDFs supports.    |
| pCDFlist    | a list of the supports of the CDFs of the p-values. Each support is represented by a vector that must be in increasing order.             |
| alpha       | the target FDP, a number strictly between 0 and 1. For <code>*</code> fast kernels, it is only necessary, if <code>stepUp = TRUE</code> . |

|                 |   |
|-----------------|---|
| zeta            | the target probability of not exceeding the desired FDP, a number strictly between 0 and 1. If zeta=NULL (the default), then zeta is chosen equal to alpha. |
| adaptive        | a boolean specifying whether to conduct an adaptive procedure or not.   |
| critical.values | a boolean. If TRUE, critical constants are computed and returned (this is computationally intensive).   |
| exact           | a boolean specifying whether to compute the Poisson-Binomial distribution exactly or by a normal approximation.   |

### Details

DPB and NDPB are wrapper functions for `discrete.PB`. The first one simply passes all its parameters to `discrete.PB` with `adaptive = TRUE` and NDPB does the same with `adaptive = FALSE`.

### Value

A FDX S3 class object whose elements are:

|                        |   |
|------------------------|---|
| Rejected               | Rejected raw p-values.  |
| Indices                | Indices of rejected hypotheses.   |
| Num.rejected           | Number of rejections.   |
| Adjusted               | Adjusted p-values (only for step-down direction).   |
| Critical.values        | Critical values (if requested).   |
| Method                 | A character string describing the used algorithm, e.g. 'Discrete Lehmann-Romano procedure (step-up)'                      |
| FDP.threshold          | FDP threshold alpha.  |
| Exceedance.probability | Probability zeta of FDP exceeding alpha; thus, FDP is being controlled at level alpha with confidence $1 - \text{zeta}$ . |
| Data\$raw.pvalues      | The values of raw.pvalues.  |
| Data\$pCDFlist         | The values of pCDFlist.   |
| Data\$data.name        | The respective variable names of raw.pvalues and pCDFlist.  |

### References

S. Döhler and E. Roquain (2019). Controlling False Discovery Exceedance for Heterogeneous Tests. [arXiv:1912.04607v1](https://arxiv.org/abs/1912.04607v1).

### See Also

[kernel](#), [FDX-package](#), [continuous.LR](#), [continuous.GR](#), [discrete.LR](#), [discrete.GR](#), [weighted.LR](#), [weighted.GR](#), [weighted.PB](#)

**Examples**

```

X1 <- c(4, 2, 2, 14, 6, 9, 4, 0, 1)
X2 <- c(0, 0, 1, 3, 2, 1, 2, 2, 2)
N1 <- rep(148, 9)
N2 <- rep(132, 9)
Y1 <- N1 - X1
Y2 <- N2 - X2
df <- data.frame(X1, Y1, X2, Y2)
df

# Construction of the p-values and their supports (fisher.pvalues.support
# is from 'DiscreteFDR' package!)
df.formatted <- fisher.pvalues.support(counts = df, input = "noassoc")
raw.pvalues <- df.formatted$raw
pCDFlist <- df.formatted$support

DPB.fast <- DPB(raw.pvalues, pCDFlist)
summary(DPB.fast)

DPB.crit <- DPB(raw.pvalues, pCDFlist, critical.values = TRUE)
summary(DPB.crit)

NDPB.fast <- NDPB(raw.pvalues, pCDFlist)
summary(NDPB.fast)

NDPB.crit <- NDPB(raw.pvalues, pCDFlist, critical.values = TRUE)
summary(NDPB.crit)

```

---

fast.Discrete

*Fast application of discrete procedures*


---

**Description**

Applies the [DLR], [DGR] or [DPB] procedures, without computing the critical values, to a data set of 2 x 2 contingency tables using Fisher's exact test.

**Usage**

```

fast.Discrete.LR(
  counts,
  alternative = "greater",
  input = "noassoc",
  alpha = 0.05,
  zeta = 0.5,
  direction = "sd",
  adaptive = TRUE
)

```

```
fast.Discrete.PB(
  counts,
  alternative = "greater",
  input = "noassoc",
  alpha = 0.05,
  zeta = 0.5,
  adaptive = TRUE,
  exact = FALSE
)
```

```
fast.Discrete.GR(
  counts,
  alternative = "greater",
  input = "noassoc",
  alpha = 0.05,
  zeta = 0.5,
  adaptive = TRUE
)
```

### Arguments

|             |   |
|-------------|---|
| counts      | a data frame of 2 or 4 columns and any number of lines, each line representing a 2 x 2 contingency table to test. The number of columns and what they must contain depend on the value of the input argument, see Details of <a href="#">fisher.pvalues.support</a> . |
| alternative | same argument as in <a href="#">fisher.test</a> . The three possible values are "greater" (default), "two.sided" or "less"; may be abbreviated.   |
| input       | the format of the input data frame, see Details of <a href="#">fisher.pvalues.support</a> . The three possible values are "noassoc" (default), "marginal" or "HG2011"; may be abbreviated.  |
| alpha       | the target FDP, a number strictly between 0 and 1. For * . fast kernels, it is only necessary, if stepUp = TRUE.  |
| zeta        | the target probability of not exceeding the desired FDP, a number strictly between 0 and 1. If zeta=NULL (the default), then zeta is chosen equal to alpha.   |
| direction   | a character string specifying whether to conduct a step-up (direction="su", the default) or step-down procedure (direction="sd").   |
| adaptive    | a boolean specifying whether to conduct an adaptive procedure or not.   |
| exact       | a boolean specifying whether to compute the Poisson-Binomial distribution exactly or by a normal approximation.   |

### Value

A FDX S3 class object whose elements are:

|              |                                 |
|--------------|---------------------------------|
| Rejected     | Rejected raw p-values.          |
| Indices      | Indices of rejected hypotheses. |
| Num.rejected | Number of rejections.           |



|                        |   |
|------------------------|---|
| Adjusted               | Adjusted p-values (only for step-down direction).   |
| Method                 | A character string describing the used algorithm, e.g. 'Discrete Lehmann-Romano procedure (step-up)'.                     |
| FDP.threshold          | FDP threshold alpha.  |
| Exceedance.probability | Probability zeta of FDP exceeding alpha; thus, FDP is being controlled at level alpha with confidence $1 - \text{zeta}$ . |
| Adaptive               | A boolean specifying whether an adaptive procedure was conducted or not.  |
| Data\$raw.pvalues      | The values of raw.pvalues.  |
| Data\$data.name        | The respective variable names of raw.pvalues and pCDFlist.  |

## Examples

```

X1 <- c(4, 2, 2, 14, 6, 9, 4, 0, 1)
X2 <- c(0, 0, 1, 3, 2, 1, 2, 2, 2)
N1 <- rep(148, 9)
N2 <- rep(132, 9)
Y1 <- N1 - X1
Y2 <- N2 - X2
df <- data.frame(X1, Y1, X2, Y2)
df

DLR.sd <- fast.Discrete.LR(counts = df, input = "noassoc")
DLR.sd$Adjusted
summary(DLR.sd)
DLR.su <- fast.Discrete.LR(counts = df, input = "noassoc", direction = "su")
summary(DLR.su)

NDLR.sd <- fast.Discrete.LR(counts = df, input = "noassoc", adaptive = FALSE)
NDLR.sd$Adjusted
summary(NDLR.sd)
NDLR.su <- fast.Discrete.LR(counts = df, input = "noassoc", direction = "su", adaptive = FALSE)
summary(NDLR.su)

DGR <- fast.Discrete.GR(counts = df, input = "noassoc")
DGR$Adjusted
summary(DGR)

NDGR <- fast.Discrete.GR(counts = df, input = "noassoc", adaptive = FALSE)
NDGR$Adjusted
summary(NDGR)

DPB <- fast.Discrete.PB(counts = df, input = "noassoc")
DPB$Adjusted
summary(DPB)

NDPB <- fast.Discrete.PB(counts = df, input = "noassoc", adaptive = FALSE)
NDPB$Adjusted

```

```
summary(NDPB)
```

---

```
hist.FDX
```

```
Histogram of Raw p-Values
```

---

## Description

Computes a histogram of the raw p-values of a FDX object.

## Usage

```
## S3 method for class 'FDX'
hist(x, breaks = "FD", main = NULL, xlab = NULL, ylab = NULL, plot = TRUE, ...)
```

## Arguments

|                         |   |
|-------------------------|---|
| <code>x</code>          | an object of class "FDX".   |
| <code>breaks</code>     | as in <a href="#">hist</a> ; here, the Friedman-Diaconis algorithm("FD") is used as default.                |
| <code>main</code>       | main title. If NULL (default), a description string is used.  |
| <code>xlab, ylab</code> | labels for x and y axis.  |
| <code>plot</code>       | a boolean If TRUE (the default), a histogram is plotted, otherwise a list of breaks and counts is returned. |
| <code>...</code>        | further arguments to <a href="#">hist</a> or <a href="#">plot.histogram</a> , respectively.                 |

## Details

If `x` contains results of a weighted approach, a histogram of the weighted p-values is constructed. Otherwise, it is constituted by the raw ones.

## Value

An object of class histogram.

## Examples

```
X1 <- c(4, 2, 2, 14, 6, 9, 4, 0, 1)
X2 <- c(0, 0, 1, 3, 2, 1, 2, 2, 2)
N1 <- rep(148, 9)
N2 <- rep(132, 9)
Y1 <- N1 - X1
Y2 <- N2 - X2
df <- data.frame(X1, Y1, X2, Y2)
df

# Construction of the p-values and their supports (fisher.pvalues.support
# is from 'DiscreteFDR' package!)
```

```
df.formatted <- fisher.pvalues.support(counts = df, input = "noassoc")
raw.pvalues <- df.formatted$raw
pCDFlist <- df.formatted$support

DGR <- DGR(raw.pvalues, pCDFlist)
hist(DGR)
```

---

kernel

*Kernel functions*


---

## Description

Kernel functions transform observed p-values or their support according to [HLR], [PB] and [HGR]. The output is used by [discrete.LR](#), [discrete.PB](#) and [discrete.GR](#), respectively. For each procedure, there is a kernel for fast computation and one for calculation of critical values. Kernels followed by ".crit", e.g. `kernel.DGR.crit`, compute and return these critical values, while kernels ending in ".fast" only transform p-values and are therefore faster. The end user should not use these functions directly.

## Usage

```
kernel_DLR_fast(
  pCDFlist,
  pvalues,
  adaptive = TRUE,
  alpha = 0.05,
  stepUp = FALSE,
  zeta = 0.5,
  support = 0L
)

kernel_DLR_crit(
  pCDFlist,
  pvalues,
  sorted_pv,
  adaptive = TRUE,
  alpha = 0.05,
  zeta = 0.5,
  stepUp = FALSE
)

kernel_DGR_fast(pCDFlist, pvalues, adaptive = TRUE, alpha = 0.05)

kernel_DGR_crit(
  pCDFlist,
  pvalues,
```

```

    sorted_pv,
    adaptive = TRUE,
    alpha = 0.05,
    zeta = 0.5
)

kernel_DPB_fast(pCDFlist, pvalues, adaptive = TRUE, alpha = 0.05, exact = TRUE)

kernel_DPB_crit(
  pCDFlist,
  pvalues,
  sorted_pv,
  adaptive = TRUE,
  alpha = 0.05,
  zeta = 0.5,
  exact = TRUE
)

kernel_wLR_fast(qvalues, weights, alpha = 0.05, geom_weighting = FALSE)

kernel_wGR_fast(qvalues, weights, alpha = 0.05, geom_weighting = FALSE)

kernel_wPB_fast(
  qvalues,
  weights,
  alpha = 0.05,
  geom_weighting = FALSE,
  exact = TRUE
)

```

### Arguments

|                        |   |
|------------------------|---|
| <code>pCDFlist</code>  | a list of the supports of the CDFs of the p-values. Each support is represented by a vector that must be in increasing order.   |
| <code>pvalues</code>   | a numeric vector. Contains all values of the p-values supports if we search for the critical constants. If not, contains only the observed p-values. Must be sorted in increasing order!            |
| <code>adaptive</code>  | a boolean specifying whether to conduct an adaptive procedure or not.   |
| <code>alpha</code>     | the target FDP, a number strictly between 0 and 1. For <code>*</code> . fast kernels, it is only necessary, if <code>stepUp = TRUE</code> .   |
| <code>stepUp</code>    | a numeric vector. Identical to <code>pvalues</code> for a step-down procedure. Equals <code>c.m</code> for a step-up procedure.   |
| <code>zeta</code>      | the target probability of not exceeding the desired FDP, a number strictly between 0 and 1. If <code>zeta=NULL</code> (the default), then <code>zeta</code> is chosen equal to <code>alpha</code> . |
| <code>support</code>   | a numeric vector. Contains all values of the p-values supports. Ignored, if <code>stepUp = FALSE</code> . Must be sorted in increasing order!   |
| <code>sorted_pv</code> | a vector of observed p-values, in increasing order.   |

|                             |   |
|-----------------------------|---|
| <code>exact</code>          | a boolean specifying whether to compute the Poisson-Binomial distribution exactly or by a normal approximation. |
| <code>qvalues</code>        | a numeric vector. Contains weighted raw p-values.   |
| <code>weights</code>        | a numeric vector. Contains the weights of the p-values.   |
| <code>geom_weighting</code> | a boolean specifying whether to conduct geometric (TRUE) or arithmetic (FALSE) weighting.                       |

### Value

For ".fast" kernels, a vector of transformed p-values is returned; ".crit" kernels return a list object with critical constants (`$crit.consts`) and transformed p-values (`$pval.transf`).

### See Also

[FDX-package](#), [discrete.LR](#), [discrete.GR](#), [discrete.PB](#), [weighted.LR](#), [weighted.GR](#), [discrete.PB](#)

### Examples

```
X1 <- c(4, 2, 2, 14, 6, 9, 4, 0, 1)
X2 <- c(0, 0, 1, 3, 2, 1, 2, 2, 2)
N1 <- rep(148, 9)
N2 <- rep(132, 9)
Y1 <- N1 - X1
Y2 <- N2 - X2
df <- data.frame(X1, Y1, X2, Y2)
df

# Construction of the p-values and their supports (fisher.pvalues.support
# is from 'DiscreteFDR' package!)
df.formatted <- fisher.pvalues.support(counts = df, input = "noassoc")
raw.pvalues <- df.formatted$raw
pCDFlist <- df.formatted$support

alpha <- 0.05

# If not searching for critical constants, we use only the observed p-values
sorted.pvals <- sort(raw.pvalues)
y.DLR.fast <- kernel_DLR_fast(pCDFlist, sorted.pvals, TRUE)
y.NDGR.fast <- kernel_DGR_fast(pCDFlist, sorted.pvals, FALSE)$pval.transf
# transformed values
y.DLR.fast
y.NDGR.fast

# compute support
pv.list <- sort(unique(unlist(pCDFlist)))
y.DGR.crit <- kernel_DGR_crit(pCDFlist, pv.list, sorted.pvals, TRUE)
y.NDPB.crit <- kernel_DPB_crit(pCDFlist, pv.list, sorted.pvals, FALSE)
# critical constants
y.DGR.crit$crit.consts
y.NDPB.crit$crit.consts
# transformed values
```

```
y.DGR.crit$pval.transf
y.NDPB.crit$pval.transf
```

---

plot.FDX

*Plot Method for FDX objects*


---

### Description

Plots raw p-values of a FDX object and highlights rejected and accepted p-values. If present, the critical values are plotted, too.

### Usage

```
## S3 method for class 'FDX'
plot(
  x,
  col = c(2, 4, 1),
  pch = c(1, 1, 1),
  lwd = c(1, 1, 1),
  type.crit = "b",
  legend = NULL,
  ...
)
```

### Arguments

|           |  |
|-----------|--|
| x         | an object of class "FDX".  |
| col       | a numeric or character vector of length 3 indicating the colors of the <ol style="list-style-type: none"> <li>rejected p-values</li> <li>accepted p-values</li> <li>critical values (if present).</li> </ol>   |
| pch       | a numeric or character vector of length 3 indicating the point characters of the <ol style="list-style-type: none"> <li>rejected p-values</li> <li>accepted p-values</li> <li>critical values (if present and type.crit is a plot type like 'p', 'b' etc.).</li> </ol> |
| lwd       | a numeric vector of length 3 indicating the thickness of the points and lines.   |
| type.crit | 1-character string giving the type of plot desired for the critical values (e.g.: 'p', 'l' etc; see <a href="#">plot</a> ).  |
| legend    | if NULL, no legend is plotted; otherwise expecting a character string like "topleft" etc. or a numeric vector of two elements indicating (x, y) coordinates.   |
| ...       | further arguments to <a href="#">plot.default</a> .  |

**Details**

If `x` contains results of a weighted approach, the Y-axis of the plot is derived from the weighted p-values. Otherwise, it is constituted by the raw ones.

**Examples**

```
X1 <- c(4, 2, 2, 14, 6, 9, 4, 0, 1)
X2 <- c(0, 0, 1, 3, 2, 1, 2, 2, 2)
N1 <- rep(148, 9)
N2 <- rep(132, 9)
Y1 <- N1 - X1
Y2 <- N2 - X2
df <- data.frame(X1, Y1, X2, Y2)
df

# Construction of the p-values and their supports (fisher.pvalues.support
# is from 'DiscreteFDR' package!)
df.formatted <- fisher.pvalues.support(counts = df, input = "noassoc")
raw.pvalues <- df.formatted$raw
pCDFlist <- df.formatted$support

DLR.sd.fast <- DLR(raw.pvalues, pCDFlist)
DLR.sd.crit <- DLR(raw.pvalues, pCDFlist, critical.values = TRUE)
DLR.su.fast <- DLR(raw.pvalues, pCDFlist, direction = "su")
DLR.su.crit <- DLR(raw.pvalues, pCDFlist, direction = "su", critical.values = TRUE)

plot(DLR.su.fast)
plot(DLR.su.crit, xlim = c(1, 5), ylim = c(0, 0.4))
plot(DLR.sd.fast, col = c(2, 4), pch = c(2, 3), lwd = c(2, 2),
     legend = "topleft", xlim = c(1, 5), ylim = c(0, 0.4))
plot(DLR.sd.crit, col = c(2, 4, 1), pch = c(1, 1, 4), lwd = c(1, 1, 2),
     type.crit = 'o', legend = c(1, 0.4), lty = 1, xlim = c(1, 5),
     ylim = c(0, 0.4))
```

---

print.FDX

*Printing FDX results*


---

**Description**

Prints the results of discrete FDX analysis, stored in a FDX S3 class object.

**Usage**

```
## S3 method for class 'FDX'
print(x, ...)
```

**Arguments**

`x` an object of class "FDX".

`...` further arguments to be passed to or from other methods. They are ignored in this function.

**Value**

The respective input object is invisibly returned via `invisible(x)`.

**Examples**

```
X1 <- c(4, 2, 2, 14, 6, 9, 4, 0, 1)
X2 <- c(0, 0, 1, 3, 2, 1, 2, 2, 2)
N1 <- rep(148, 9)
N2 <- rep(132, 9)
Y1 <- N1 - X1
Y2 <- N2 - X2
df <- data.frame(X1, Y1, X2, Y2)
df

# Construction of the p-values and their supports (fisher.pvalues.support
# is from 'DiscreteFDR' package!)
df.formatted <- fisher.pvalues.support(counts = df, input = "noassoc")
raw.pvalues <- df.formatted$raw
pCDFlist <- df.formatted$support

DPB.crit <- DPB(raw.pvalues, pCDFlist, critical.values = TRUE)
print(DPB.crit)
```

---

rejection.path

*Rejection Path Plot (for FDX objects)*


---

**Description**

Displays the number of rejections of the raw p-values in a FDX object in dependence of the exceedance probability  $\zeta$ .

**Usage**

```
rejection.path(
  x,
  xlim = NULL,
  ylim = NULL,
  main = NULL,
  xlab = expression(zeta),
  ylab = "Number of Rejections",
  verticals = FALSE,
```



```

    pch = 19,
    ref.show = FALSE,
    ref.col = "gray",
    ref.lty = 2,
    ref.lwd = 2,
    ...
  )

```

### Arguments

|                               |  |
|-------------------------------|--|
| <code>x</code>                | an object of class "FDX".  |
| <code>xlim</code>             | the x limits of the plot. If NULL (default), the (0, 1) range is used.   |
| <code>ylim</code>             | the y limits of the plot. If NULL (default), the double of the median of the number of possible rejections is used as upper limit.                 |
| <code>main</code>             | main title. If NULL (default), a description string is used.   |
| <code>xlab, ylab</code>       | labels for x and y axis.   |
| <code>verticals</code>        | logical; if TRUE, draw vertical lines at steps.  |
| <code>pch</code>              | jump point character.  |
| <code>ref.show</code>         | logical; if TRUE a vertical reference line is plotted, whose height is the number of rejections of the original Benjamini-Hochberg (BH) procedure. |
| <code>ref.col</code>          | color of the reference line.   |
| <code>ref.lty, ref.lwd</code> | line type and thickness for the reference line.  |
| <code>...</code>              | further arguments to <a href="#">plot.stepfun</a> .  |

### Value

Invisibly returns a stepfun object that computes the number of rejections in dependence on the exceedance probability  $\zeta$ .

### Examples

```

X1 <- c(4, 2, 2, 14, 6, 9, 4, 0, 1)
X2 <- c(0, 0, 1, 3, 2, 1, 2, 2, 2)
N1 <- rep(148, 9)
N2 <- rep(132, 9)
Y1 <- N1 - X1
Y2 <- N2 - X2
df <- data.frame(X1, Y1, X2, Y2)
df

# Construction of the p-values and their supports (fisher.pvalues.support
# is from 'DiscreteFDR' package!)
df.formatted <- fisher.pvalues.support(counts = df, input = "noassoc")
raw.pvalues <- df.formatted$raw
pCDFlist <- df.formatted$support

DLR <- DLR(raw.pvalues, pCDFlist)

```

```

NDLR <- NDLR(raw.pvalues, pCDFlist)

rejection.path(DLR, xlim = c(0, 1), ref.show = TRUE, ref.col = "green", ref.lty = 4)
rejection.path(NDLR, col = "red", add = TRUE)

```

---

summary.FDX

*Summarizing Discrete FDX Results*


---

## Description

summary method for class "FDX"

## Usage

```

## S3 method for class 'FDX'
summary(object, ...)

## S3 method for class 'summary.FDX'
print(x, max = NULL, ...)

```

## Arguments

|        |   |
|--------|---|
| object | an object of class "FDX".   |
| ...    | further arguments passed to or from other methods.  |
| x      | an object of class "summary.FDX".   |
| max    | numeric or NULL, specifying the maximal number of <i>rows</i> of the p-value table to be printed. By default, when NULL, <code>getOption("max.print")</code> is used. |

## Details

summary.FDX objects include all data of an FDX object, but also include an additional table which includes the raw p-values, their indices, the respective critical values (if present), the adjusted p-values (if present) and a logical column to indicate rejection. The table is sorted in ascending order by the raw p-values.

print.summary.FDX simply prints the same output as print.FDX, but also prints the p-value table.

## Value

summary.FDX computes and returns a list that includes all the data of an input FDX, plus

|       |  |
|-------|--|
| Table | a data.frame, sorted by the raw p-values, that contains the indices, that raw p-values themselves, their respective critical values (if present), their adjusted p-values (if present) and a logical column to indicate rejection. |
|-------|--|

print.summary.FDX returns that object invisibly.

**Examples**

```

X1 <- c(4, 2, 2, 14, 6, 9, 4, 0, 1)
X2 <- c(0, 0, 1, 3, 2, 1, 2, 2, 2)
N1 <- rep(148, 9)
N2 <- rep(132, 9)
Y1 <- N1 - X1
Y2 <- N2 - X2
df <- data.frame(X1, Y1, X2, Y2)
df

# Construction of the p-values and their supports (fisher.pvalues.support
# is from 'DiscreteFDR' package!)
df.formatted <- fisher.pvalues.support(counts = df, input = "noassoc")
raw.pvalues <- df.formatted$raw
pCDFlist <- df.formatted$support

DGR.crit <- DGR(raw.pvalues, pCDFlist, critical.values = TRUE)
DGR.crit.summary <- summary(DGR.crit)
print(DGR.crit.summary)

```

---

weighted.GR

*Weighted Guo-Romano Procedure*


---

**Description**

Apply the weighted [wGR] procedure, with or without computing the critical values, to a set of p-values. Both arithmetic and geometric weighting are available.

**Usage**

```

weighted.GR(
  raw.pvalues,
  weights,
  alpha = 0.05,
  zeta = 0.5,
  weighting.method = "AM",
  critical.values = FALSE
)

wGR.AM(raw.pvalues, weights, alpha = 0.05, zeta = 0.5, critical.values = FALSE)

wGR.GM(raw.pvalues, weights, alpha = 0.05, zeta = 0.5, critical.values = FALSE)

```

**Arguments**

`raw.pvalues` vector of the raw observed p-values, as provided by the end user and before matching with their nearest neighbor in the CDFs supports.

|                  |   |
|------------------|---|
| weights          | a numeric vector. Contains the weights of the p-values.   |
| alpha            | the target FDP, a number strictly between 0 and 1. For <code>*</code> fast kernels, it is only necessary, if <code>stepUp = TRUE</code> .   |
| zeta             | the target probability of not exceeding the desired FDP, a number strictly between 0 and 1. If <code>zeta=NULL</code> (the default), then <code>zeta</code> is chosen equal to <code>alpha</code> . |
| weighting.method | a character string specifying whether to conduct arithmetic ( <code>direction="AM"</code> , the default) or geometric weighting ( <code>direction="GM"</code> ) of p-values.                        |
| critical.values  | a boolean. If <code>TRUE</code> , critical constants are computed and returned (this is computationally intensive).   |

### Details

`wGR.AM` and `wGR.GM` are wrapper functions for `weighted.GR`. The first one simply passes all its parameters to `weighted.GR` with `weighting.method = "AM"` and `wGR.GM` does the same with `weighting.method = "GM"`.

### Value

A `FDX S3` class object whose elements are:

|                        |   |
|------------------------|---|
| Rejected               | Rejected raw p-values.  |
| Indices                | Indices of rejected hypotheses.   |
| Num.rejected           | Number of rejections.   |
| Adjusted               | Adjusted p-values (only for step-down direction).   |
| Weighted               | Weighted p-values.  |
| Critical.values        | Critical values (if requested).   |
| Method                 | A character string describing the used algorithm, e.g. 'Discrete Lehmann-Romano procedure (step-up)'  |
| FDP.threshold          | FDP threshold <code>alpha</code> .  |
| Exceedance.probability | Probability <code>zeta</code> of FDP exceeding <code>alpha</code> ; thus, FDP is being controlled at level <code>alpha</code> with confidence <code>1 - zeta</code> . |
| Weighting              | A character string describing the weighting method.   |
| Data\$raw.pvalues      | The values of <code>raw.pvalues</code> .  |
| Data\$weights          | The values of <code>weights</code> .  |
| Data\$data.name        | The respective variable names of <code>raw.pvalues</code> and <code>pCDFlist</code> .   |

### References

S. Döhler and E. Roquain (2019). Controlling False Discovery Exceedance for Heterogeneous Tests. [arXiv:1912.04607v1](https://arxiv.org/abs/1912.04607v1).

**See Also**

[kernel](#), [FDX-package](#), [continuous.LR](#), [continuous.GR](#), [discrete.LR](#), [discrete.GR](#), [discrete.PB](#), [weighted.LR](#), [weighted.PB](#)

**Examples**

```
# Construction of the p-values and their supports for weighted methods
raw.pvalues.weighted <- c(0.7389727, 0.1882310, 0.1302457, 0.9513677,
                        0.7592122, 0.0100559, 0.0000027, 0.1651034)
weights <- c(0.7947122, 1.2633867, 2.8097858, 2.2112801,
            2.3878654, 1.2389620, 2.3878654, 0.7947122)

wGR.AM.fast <- wGR.AM(raw.pvalues.weighted, weights)
summary(wGR.AM.fast)

wGR.AM.crit <- wGR.AM(raw.pvalues.weighted, weights, critical.values = TRUE)
summary(wGR.AM.crit)

wGR.GM.fast <- wGR.GM(raw.pvalues.weighted, weights)
summary(wGR.GM.fast)

wGR.GM.crit <- wGR.GM(raw.pvalues.weighted, weights, critical.values = TRUE)
summary(wGR.GM.crit)
```

---

 weighted.LR

*Weighted Lehmann-Romano Procedure*


---

**Description**

Apply the weighted [wLR] procedure, with or without computing the critical values, to a set of p-values. Both arithmetic and geometric weighting are available.

**Usage**

```
weighted.LR(
  raw.pvalues,
  weights,
  alpha = 0.05,
  zeta = 0.5,
  weighting.method = "AM",
  critical.values = FALSE
)

wLR.AM(raw.pvalues, weights, alpha = 0.05, zeta = 0.5, critical.values = FALSE)

wLR.GM(raw.pvalues, weights, alpha = 0.05, zeta = 0.5, critical.values = FALSE)
```

**Arguments**

|                  |   |
|------------------|---|
| raw.pvalues      | vector of the raw observed p-values, as provided by the end user and before matching with their nearest neighbor in the CDFs supports.  |
| weights          | a numeric vector. Contains the weights of the p-values.   |
| alpha            | the target FDP, a number strictly between 0 and 1. For <code>*</code> fast kernels, it is only necessary, if <code>stepUp = TRUE</code> .   |
| zeta             | the target probability of not exceeding the desired FDP, a number strictly between 0 and 1. If <code>zeta=NULL</code> (the default), then <code>zeta</code> is chosen equal to <code>alpha</code> . |
| weighting.method | a character string specifying whether to conduct arithmetic ( <code>direction="AM"</code> , the default) or geometric weighting ( <code>direction="GM"</code> ) of p-values.                        |
| critical.values  | a boolean. If <code>TRUE</code> , critical constants are computed and returned (this is computationally intensive).   |

**Details**

`wLR.AM` and `wLR.GM` are wrapper functions for `weighted.LR`. The first one simply passes all its parameters to `weighted.LR` with `weighting.method = "AM"` and `wLR.GM` does the same with `weighting.method = "GM"`.

**Value**

A FDX S3 class object whose elements are:

|                        |   |
|------------------------|---|
| Rejected               | Rejected raw p-values.  |
| Indices                | Indices of rejected hypotheses.   |
| Num.rejected           | Number of rejections.   |
| Adjusted               | Adjusted p-values (only for step-down direction).   |
| Weighted               | Weighted p-values.  |
| Critical.values        | Critical values (if requested).   |
| Method                 | A character string describing the used algorithm, e.g. 'Discrete Lehmann-Romano procedure (step-up)'.   |
| FDP.threshold          | FDP threshold <code>alpha</code> .  |
| Exceedance.probability | Probability <code>zeta</code> of FDP exceeding <code>alpha</code> ; thus, FDP is being controlled at level <code>alpha</code> with confidence <code>1 - zeta</code> . |
| Weighting              | A character string describing the weighting method.   |
| Data\$raw.pvalues      | The values of <code>raw.pvalues</code> .  |
| Data\$weights          | The values of <code>weights</code> .  |
| Data\$data.name        | The respective variable names of <code>raw.pvalues</code> and <code>pCDFlist</code> .   |

**See Also**

[kernel](#), [FDX-package](#), [continuous.LR](#), [continuous.GR](#), [discrete.LR](#), [discrete.GR](#), [discrete.PB](#), [weighted.GR](#), [weighted.PB](#)

**Examples**

```
# Construction of the p-values and their supports for weighted methods
raw.pvalues.weighted <- c(0.7389727, 0.1882310, 0.1302457, 0.9513677,
  0.7592122, 0.0100559, 0.0000027, 0.1651034)
weights <- c(0.7947122, 1.2633867, 2.8097858, 2.2112801,
  2.3878654, 1.2389620, 2.3878654, 0.7947122)

wLR.AM.fast <- wLR.AM(raw.pvalues.weighted, weights)
summary(wLR.AM.fast)

wLR.AM.crit <- wLR.AM(raw.pvalues.weighted, weights, critical.values = TRUE)
summary(wLR.AM.crit)

wLR.GM.fast <- wLR.GM(raw.pvalues.weighted, weights)
summary(wLR.GM.fast)

wLR.GM.crit <- wLR.GM(raw.pvalues.weighted, weights, critical.values = TRUE)
summary(wLR.GM.crit)
```

---

 weighted.PB

---

*Weighted Poisson-Binomial Procedure*


---

**Description**

Apply the weighted [wPB] procedure, with or without computing the critical values, to a set of p-values. Both arithmetic and geometric weighting are available. Additionally, the user can choose between exact computation of the Poisson-Binomial distribution or a refined normal approximation.

**Usage**

```
weighted.PB(
  raw.pvalues,
  weights,
  alpha = 0.05,
  zeta = 0.05,
  weighting.method = "AM",
  critical.values = FALSE,
  exact = TRUE
)

wPB.AM(raw.pvalues, weights, alpha = 0.05, zeta = 0.5, critical.values = FALSE)

wPB.GM(raw.pvalues, weights, alpha = 0.05, zeta = 0.5, critical.values = FALSE)
```

**Arguments**

|                  |   |
|------------------|---|
| raw.pvalues      | vector of the raw observed p-values, as provided by the end user and before matching with their nearest neighbor in the CDFs supports.  |
| weights          | a numeric vector. Contains the weights of the p-values.   |
| alpha            | the target FDP, a number strictly between 0 and 1. For <code>*</code> .fast kernels, it is only necessary, if <code>stepUp = TRUE</code> .  |
| zeta             | the target probability of not exceeding the desired FDP, a number strictly between 0 and 1. If <code>zeta=NULL</code> (the default), then <code>zeta</code> is chosen equal to <code>alpha</code> . |
| weighting.method | a character string specifying whether to conduct arithmetic ( <code>direction="AM"</code> , the default) or geometric weighting ( <code>direction="GM"</code> ) of p-values.                        |
| critical.values  | a boolean. If <code>TRUE</code> , critical constants are computed and returned (this is computationally intensive).   |
| exact            | a boolean specifying whether to compute the Poisson-Binomial distribution exactly or by a normal approximation.   |

**Details**

`wPB.AM` and `wPB.GM` are wrapper functions for `weighted.PB`. The first one simply passes all its parameters to `weighted.PB` with `weighting.method = "AM"` and `wPB.GM` does the same with `weighting.method = "GM"`.

**Value**

A FDX S3 class object whose elements are:

|                        |   |
|------------------------|---|
| Rejected               | Rejected raw p-values.  |
| Indices                | Indices of rejected hypotheses.   |
| Num.rejected           | Number of rejections.   |
| Adjusted               | Adjusted p-values (only for step-down direction).   |
| Weighted               | Weighted p-values.  |
| Critical.values        | Critical values (if requested).   |
| Method                 | A character string describing the used algorithm, e.g. 'Discrete Lehmann-Romano procedure (step-up)'  |
| FDP.threshold          | FDP threshold <code>alpha</code> .  |
| Exceedance.probability | Probability <code>zeta</code> of FDP exceeding <code>alpha</code> ; thus, FDP is being controlled at level <code>alpha</code> with confidence $1 - \text{zeta}$ . |
| Weighting              | A character string describing the weighting method.   |
| Data\$raw.pvalues      | The values of <code>raw.pvalues</code> .  |
| Data\$weights          | The values of <code>weights</code> .  |
| Data\$data.name        | The respective variable names of <code>raw.pvalues</code> and <code>pCDFlist</code> .   |



**See Also**

[kernel](#), [FDX-package](#), [continuous.LR](#), [continuous.GR](#), [discrete.LR](#), [discrete.GR](#), [discrete.PB](#), [weighted.LR](#), [weighted.GR](#)

**Examples**

```
# Construction of the p-values and their supports for weighted methods
raw.pvalues.weighted <- c(0.7389727, 0.1882310, 0.1302457, 0.9513677,
  0.7592122, 0.0100559, 0.0000027, 0.1651034)
weights <- c(0.7947122, 1.2633867, 2.8097858, 2.2112801,
  2.3878654, 1.2389620, 2.3878654, 0.7947122)

wPB.AM.fast <- wPB.AM(raw.pvalues.weighted, weights)
summary(wPB.AM.fast)

wPB.AM.crit <- wPB.AM(raw.pvalues.weighted, weights, critical.values = TRUE)
summary(wPB.AM.crit)

wPB.GM.fast <- wPB.GM(raw.pvalues.weighted, weights)
summary(wPB.GM.fast)

wPB.GM.crit <- wPB.GM(raw.pvalues.weighted, weights, critical.values = TRUE)
summary(wPB.GM.crit)
```

# Index

## \* datasets

amnesia, 3

amnesia, 3

continuous.GR, 4, 7, 9, 12, 14, 29, 31, 33

continuous.LR, 5, 6, 9, 12, 14, 29, 31, 33

DGR (discrete.GR), 8

discrete.GR, 5, 7, 8, 12, 14, 19, 21, 29, 31, 33

discrete.LR, 5, 7, 9, 10, 14, 19, 21, 29, 31, 33

discrete.PB, 5, 7, 9, 12, 13, 19, 21, 29, 31, 33

DLR (discrete.LR), 10

DPB (discrete.PB), 13

fast.Discrete, 15

FDX-package, 2

fisher.pvalues.support, 2, 16

fisher.test, 16

GR (continuous.GR), 4

hist, 18

hist.FDX, 18

kernel, 5, 7, 9, 12, 14, 19, 29, 31, 33

kernel\_DGR\_crit (kernel), 19

kernel\_DGR\_fast (kernel), 19

kernel\_DLR\_crit (kernel), 19

kernel\_DLR\_fast (kernel), 19

kernel\_DPB\_crit (kernel), 19

kernel\_DPB\_fast (kernel), 19

kernel\_wGR\_fast (kernel), 19

kernel\_wLR\_fast (kernel), 19

kernel\_wPB\_fast (kernel), 19

LR (continuous.LR), 6

NDGR (discrete.GR), 8

NDLR (discrete.LR), 10

NDPB (discrete.PB), 13

NGR (continuous.GR), 4

NLR (continuous.LR), 6

plot, 22

plot.default, 22

plot.FDX, 22

plot.histogram, 18

plot.stepfun, 25

print.FDX, 23

print.summary.FDX (summary.FDX), 26

rejection.path, 24

summary.FDX, 26

weighted.GR, 5, 7, 9, 12, 14, 21, 27, 31, 33

weighted.LR, 5, 7, 9, 12, 14, 21, 29, 29, 33

weighted.PB, 5, 7, 9, 12, 14, 29, 31, 31

wGR.AM (weighted.GR), 27

wGR.GM (weighted.GR), 27

wLR.AM (weighted.LR), 29

wLR.GM (weighted.LR), 29

wPB.AM (weighted.PB), 31

wPB.GM (weighted.PB), 31